Example questions

In how many ways can 1 gold, 1 silver, and 1 bronze metal be awarded to 10 contestants? P(10,3)=10x9x8=720

How many ways are there to select 3 class representatives from a class of 25 students?

You can borrow up to 3 DVDs from your friends, who owns 30 DVDs.

- How many ways are there to select 1 DVD?
 C(30,1)=30
- How many ways are there to select 2 DVDs? $C(30,2) = \frac{30!}{28!2!} = \frac{30 \times 29}{2 \times 1} = 30 \times 29/2 = 15 \times 29 = 435$
- How many ways are there to select 3 DVDs? $C(30,3) = \frac{30 \times 29 \times 28}{3 \times 2 \times 1} = 30 \times 29 \times 28 / 6 = 5 \times 29 \times 28 = 4060$
- How many ways are there to select 3 or fewer DVDs?
 C(30,3)+C(30,2)+C(30,1)+C(30,0)=4060+435+30+1=4526

There are 8 songs you can play at your party. How many ways are there to select a play list containing 5 of these songs (where the order matters)?

You are taking a multiple choice test where each question has 5 possible answers to choose from --- A, B, C, D, or E --- and there are 4 questions in total.

- How many possible ways are there to select your answers?
- How many ways are there to select answers if no letter can be used for more than one question?
- How many ways are there to select answers if the fourth answer must by the same as the first?
 5x5x5x1=125
- How many ways are there to select answers if one letter is used for two of the answers and the remaining answers use distinct letters?

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- in first, second, and third edition
- for overnight, 2-day, and 5-day delivery

How many ways can you order the computer science book?

I am forming a Fordham Jeopardy team and need to select 6 members. I have 7 candidates from the Computer Science department, 9 from the Economics department, 10 from the English department, and 12 from the Theater department.

(Give the expression to find the answers, actual number is welcome but not required)

- How many ways can I choose from all the candidates?
- How many ways can I choose a team where all members are from the same department?
- How many ways can I choose a team with 2 computer science students, 2 economics students, and 2 theatre students?

$$C(7,2)+C(9,2)+C(12,2)=\frac{7!}{5!2!}+\frac{9!}{7!2!}+\frac{12!}{10!2!}=7x6/2+9x8/2+12x11/2=7x3+9x4+6x11=21+36+66=123$$

• How many ways can I choose a team with no computer science majors?

Solve for:

P(3,1)

P(4,2)=4x3=12

P(5,2)

P(m,0)

$$C(5,3) = \frac{5!}{3!2!} = \frac{5 \times 4 \times 3}{3 \times 2 \times 1} = 5 \times 4 \times 3 / 6 = 60 / 6 = 10$$

C(4,1)=4/1!=4

C(4,4)

You are given an exam with every question having either the answer "true" or "false." There are 10 questions on the exam and you guess randomly for each question. Assuming each answer is equally likely to be true or false:

- What is the probability you get exactly 5 questions correct?
- What is the probability you get fewer than 8 questions correct? 1-Prob(get 8 or more correct)

Prob(get 8 or more correct)=Prob(exactly 8 correct)+Prob(exactly 9 correct)

+Prob(exactly 10 correct)

Prob(exactly 8 correct)=C(10,8)/2¹⁰=45/2¹⁰ (arrangements of CCCCCCCII,

where C is "correct" and I is "incorrect")

Prob(exactly 9 correct)=C(10,9)/2¹⁰=10/2¹⁰

Prob(exactly 10 correct)= $C(10,10)=1/2^{10}$

$$1 - \frac{(45+10+1)}{2^{10}} = 1 - \frac{56}{2^{10}} = \frac{972}{1028} + \frac{968}{1024} \approx .945$$

You have a jar of jelly beans in front of you containing 20 cherry, 10 orange, 15 lemon, 15 watermelon, and 10 grape flavor. You take 5 beans without looking.

(Give the expression to find the answers, actual number/fraction is welcome but not required):

- What is the probability you pick one of each flavor?
- What is the probability none of the picked beans are cherry?

We go to the casino and play a dice-rolling game. Each die is 6 sided and 3 die are rolled.

- What is the probability all 3 die roll higher than 4?
- What is the probability at least one 3 is rolled?

Prob(exactly one 3)+Prob(exactly two 3s)+Prob(exactly three 3s)=
$$\frac{\frac{3\times(1\times5\times5)+3\times(1\times1\times5)+1}{216}}{\frac{216}{216}} = \frac{\frac{7}{216}}{\frac{216}{216}}$$

- What is the probability all 3 rolls are different?
- What is the probability the first 2 dice rolled add up to 2 or 5?
- What is the probability the first roll is even or greater than 4? Prob(even)+Prob(greater than 4)-Prob(even and greater than 4)=

$$\frac{3}{6} + \frac{2}{6} - \frac{1}{6} = \frac{4}{6} = \frac{2}{3}$$

What is the probability the second roll is a multiple of 2 or of 3?

I flip a biased coin where it will land on heads with 2/3 probability.

- What is the probability of getting 2 tails in 2 flips?
- What is the probability of getting all heads in 4 flips? Prob(first head)xProb(second head)xProb(third head)xProb(fourth head)=

$$\frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} = \frac{8}{81} \qquad \frac{16}{81}$$
• What is the probability of getting fewer than 2 tails in 4 flips?