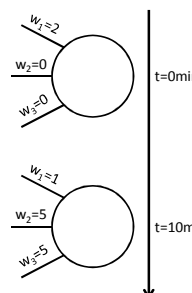


CISC 3250 Systems Neuroscience

**Neuroplasticity:
Learning in Neurons**

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JMH 328A



t=0min

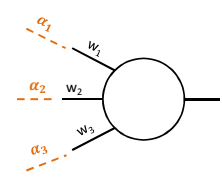
t=10min

Review of weights




$R_i(t) = \sum_j w_j \alpha_j(t)$

Weights indicate


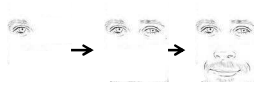
- Connection (0 or not)
- NT effect
 - $w > 0$ excitatory
 - $w < 0$ inhibitory
- Magnitude of impact of input



Association

- We recall information through associations with other information
- Pneumonics:
 - Roy G. Biv
 - Please Excuse My Dear Aunt Sally () Exp x / + -
- Memories of experiences:
 - Lake -> Summer vacation 2012 
 - Dealy -> Final exam Fall 2014 
- Complex objects
 - ::Bark:: -> Dog, fur, happy/fear 

Features of associators

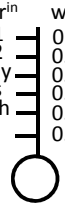

- Pattern completion/ generalization 
- Fault tolerance
 - Selected dendrites miss input, post-synaptic neuron still fires
- Learning prototypes
 - Neuron firing for common combinations 

Pattern completion

Activation requires only a subset of desired inputs

r^{in}	w
leg1	0.5
leg2	0.5
body	0.5
ears	0.5
mouth	0.5
tail	0.5

How many inputs needed to fire?

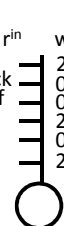
Define input $h = \sum_i w_i r_i^{in}$
 Neuron fires at rate $r^{out}=1$ when $h > 1.5$
 Assume $r^{in}=1$ when active, $r^{in}=0$ when inactive

Fault tolerance

Activation requires only a subset of desired inputs

r^{in}	w
moo	2
quack	0
woof	0
woof	2
woof	0
moo	2

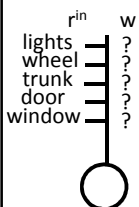
How many inputs needed to fire?



$h = \sum_i w_i r_i^{in}$
 Neuron fires at rate $r^{out}=1$ when $h > 1.5$

Prototypes

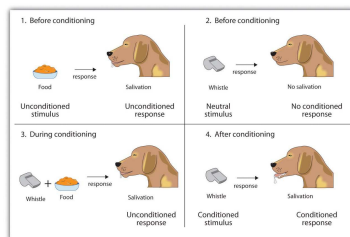
Activation requires all desired inputs



$$h = \sum_i w_i r_i^{in}$$

Neuron fires at rate $r^{out}=1$ when $h > 1.5$

Learning to associate: Conditioning



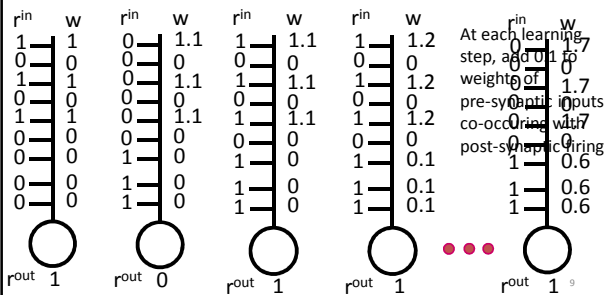
Associating both smell and whistle with food

- **Unconditioned stimulus:** smell – already associated with food
- **Conditioned stimulus:** whistle – indicates food coming

Computing level: Associator network

Define input $h = \sum_j w_j r_j^{in}$

Neuron fires at rate $r^{out}=1$ when $h > 1.5$



Two forms of plasticity

- **Structural plasticity:** generation of new connections between neurons
- **Functional plasticity:** changing strength of connections between neurons

Hebbian plasticity:
“cells that fire together, wire together”

Chemical level: NT receptors

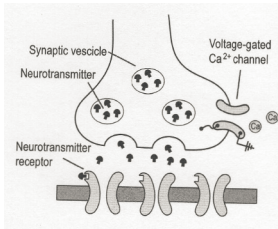
Increase weight by improving NT detection

Post-synaptic:

- Insert more receptors into dendrite membrane
- Improve performance of receptors

Pre-synaptic:

- Increase amount of NT released



Marr's levels of analysis

- **Computational theory:** Learn associations among sensations
- **Representation and algorithm:** Associate each sense with set of neural outputs, adjust weights on these outputs into another neuron
- **Hardware implementation:** Insert/remove NT receptors from dendrites

Math of Hebbian rate learning

“Cells that fire together, wire together”

$r_i \rightarrow r^{out}$
 $r_j \rightarrow r^{in}$
 ϵ learning speed

$$\Delta w_{ij} = \epsilon(w) r_i r_j$$

Time (sec)

Using the learning rule

Define input $h = \sum_j w_j r_j^{in}$
 Neuron fires at rate $r^{out}=1$ when $h > 1$

$$\epsilon(w) = \begin{cases} -0.5 & w < 0 \\ 0.5 & w \geq 0 \end{cases}$$

$$\Delta w_{ij} = \epsilon(w) r_i r_j$$

r^{in} w r^{in} w r^{in} w r^{in} w
 $r^{out}=1$ $r^{out}=1$ $r^{out}=1$ $r^{out}=1$

Weight control and decay

- Synaptic weights are finite
- Propose learning rules that keep weights bounded

$$\Delta w_{ij} = r_i r_j - c w_{ij}$$

$$\Delta w_{ij} = r_i (r_j - w_{ij}) - \text{Willshaw}$$

- Or, preserve total synaptic weight across network: “normalization”

$$w_{ij} \leftarrow \frac{w_{ij}}{\sum_j w_{ij}}$$

Using weight control and decay

Define input $h = \sum_j w_j r_j^{in}$
 Neuron fires at rate $r^{out}=1$ when $h > 1$

$$\Delta w_{ij} = r_i (r_j - w_{ij})$$

r^{in} w r^{in} w r^{in} w r^{in} w
 $r^{out}=0$ $r^{out}=1$ $r^{out}=1$ $r^{out}=1$

Using weight control and decay

Define input $h = \sum_j w_j r_j^{in}$
 Neuron fires at rate $r^{out}=1$ when $h > 1$

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r^{in} w r^{in} w r^{in} w r^{in} w
 $r^{out}=0$ $r^{out}=0$ $r^{out}=0$ $r^{out}=0$