

CISC 3250 Systems Neuroscience

Representations in the brain



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JMH 328A

How do we represent our world? Diverse sensations

Dog



- Body parts
 - tail, ears, legs
- Sounds
 - bark, whimper, pant
- Feel
 - fur

Flower



- Appearance
 - color, size, shape
- Smell
- Feel
 - texture, temperature

We call each piece of
information a "feature"

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How do we represent our world? One sensation, multiple levels

Song

- Meaning of words
- Pitch/melody
- Rhythm
- Language
- Singer identity

Dance

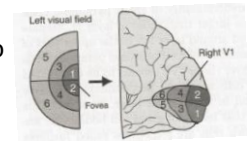
- Body part
 - arms, hands, legs
- Direction
 - forward, to-the-left
- Timing
 - order of moves, speed



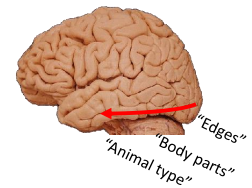
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Data in the brain

- Neural location related to information encoded



- Progression of encoding for increasingly complex concepts



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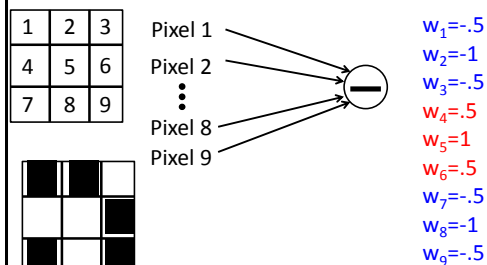
Simple outline of vision pathway

1. Retina: pixel detectors
2. Primary visual cortex (V1): edge detectors
3. Second-cortical layer (V2?): edge combination detectors
- ...
- N. Higher-cortical layer: Full-object detectors

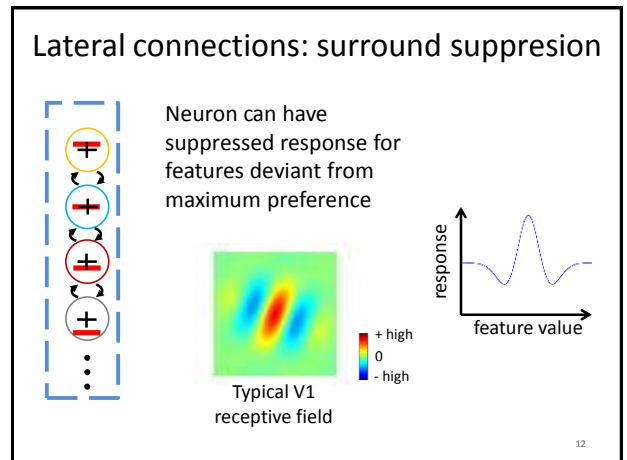
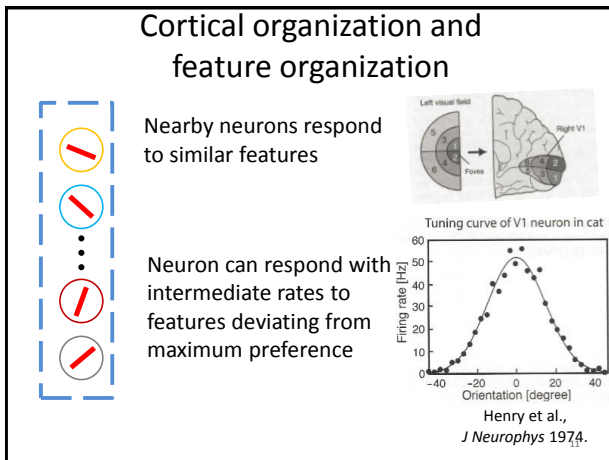
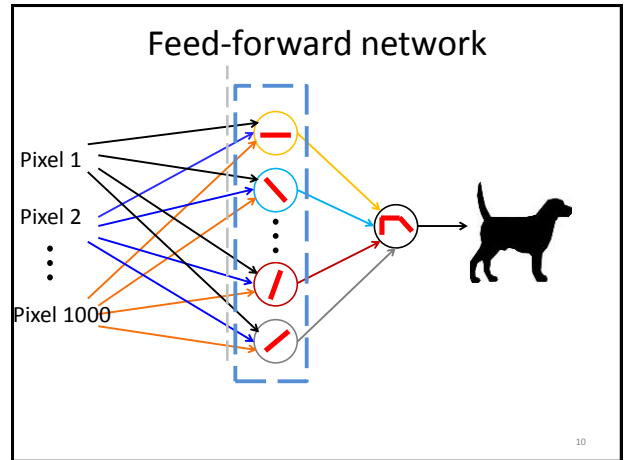
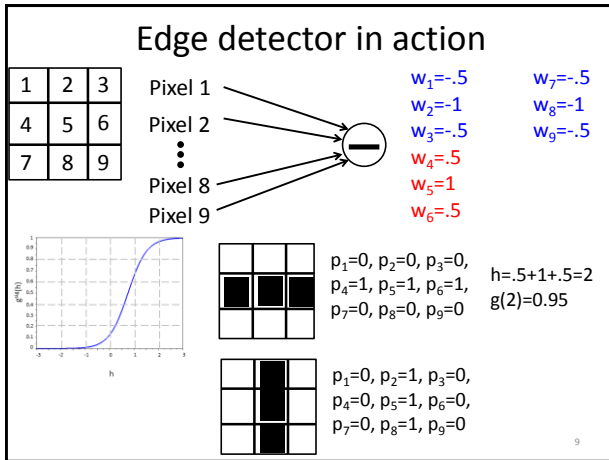
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Interacting representations: feedforward network

- More-complex information/features computed from simpler information/features



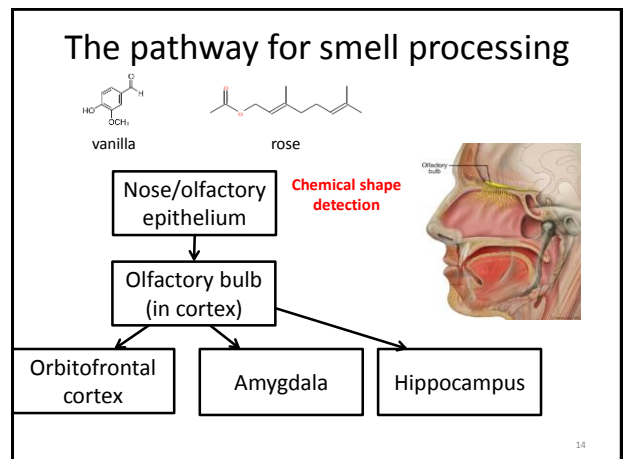
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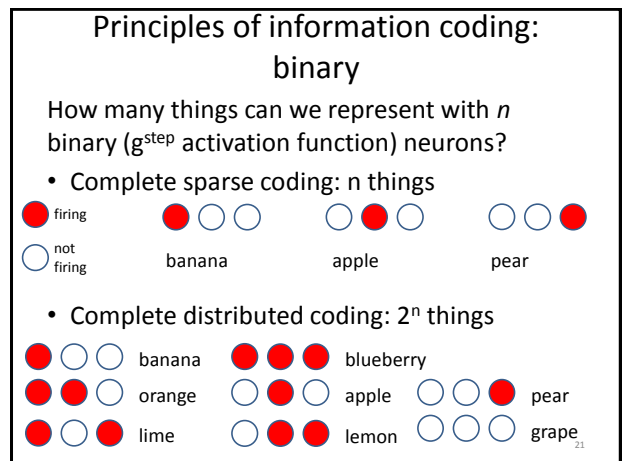
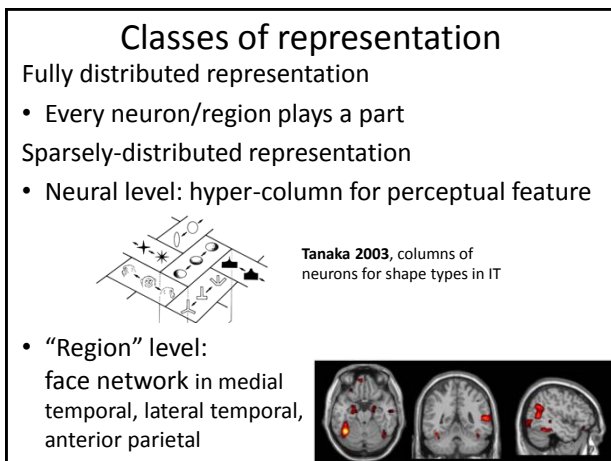
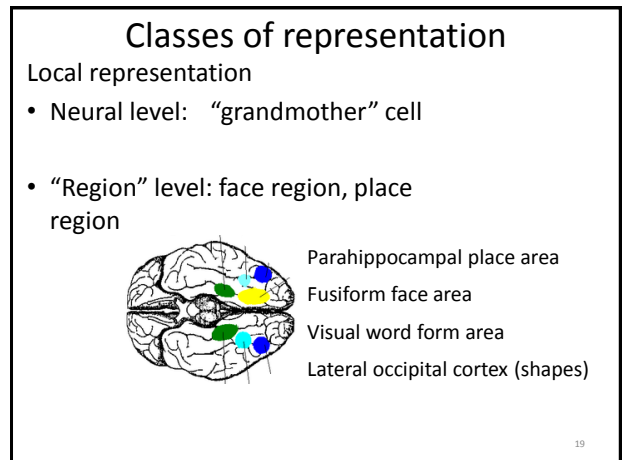
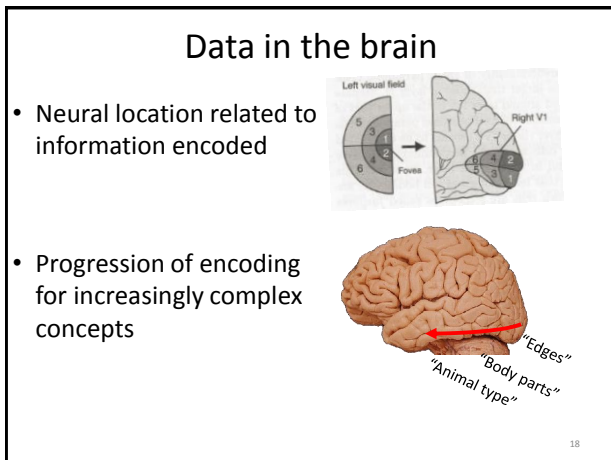
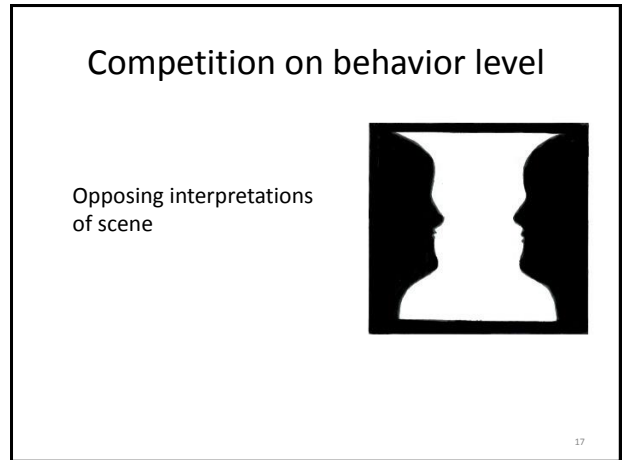
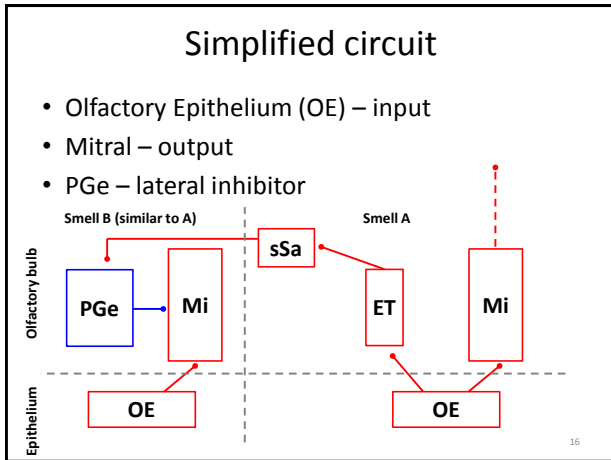


Suppression/competition with interneurons

- In common cortical circuits, there are feedforward excitatory inputs and lateral inhibitory inputs
- Relative weighting achieves balance between activation and suppression

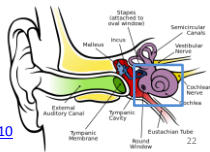
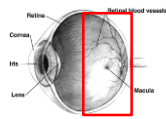
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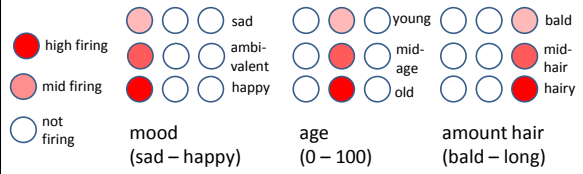
Biology of sparse coding

- Preserving energy – higher spiking rate requires higher energy
- Representational fan-out
 - ~1 million neurons in retina ->
 - ~140 million neurons in V1 (primary visual cortex)
 - ~50,000 neurons in cochlea ->
 - 1.6 million neurons in A1 (primary auditory cortex)



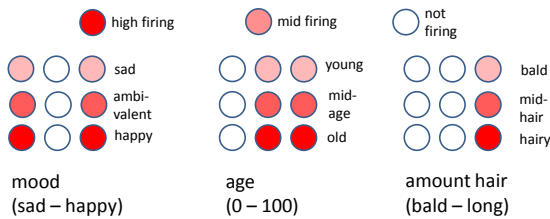
<http://www.plosbiology.org/article/info:doi/10.1371/journal.pbio.0030137>

Coding on a scale: sparsity



Typically we will say "sparsity" is using at most 10% of available neurons

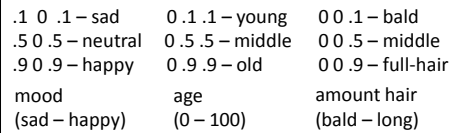
Coding on a scale: distributed + overlapping



What does this encode?

Coding on a scale: distributed + overlapping

Responses for each property add together

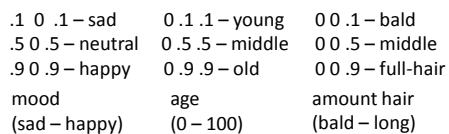


What does this encode? 0 .4 .8

What does this encode? 1 .5 1.5

Coding on a scale: distributed + overlapping

Responses for each property add together

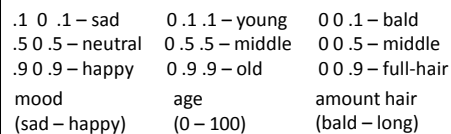


What does this encode? 0 .4 .8
Very sad: contributes: $0 \times [1 \ 0 \ 1] = 0 \ 0 \ 0$
Middle-age: contributes $.4 \times [0 \ 1 \ 1] = 0 \ .4 \ .4$
Middle-hair: contributes $.4 \times [0 \ 0 \ 1] = 0 \ 0 \ .4$
Summing together: 0 .4 .8

Neuron 1
Neuron 2
Neuron 3

Coding on a scale: distributed + overlapping

Responses for each property add together



What does this encode? 1 .5 1.5
Very happy: contributes $1 \times [1 \ 0 \ 1] = 1 \ 0 \ 1$
Middle-age: contributes $.5 \times [0 \ 1 \ 1] = 0 \ .5 \ .5$
Bald: contributes $0 \times [0 \ 0 \ 1] = 0 \ 0 \ 0$
Summing together: 1 .5 1.5

Neuron 1
Neuron 2
Neuron 3

Coding on a scale: distributed + overlapping

Responses for each property add together

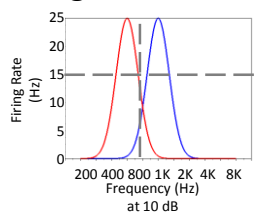
.1 0 .1 – sad	0 .1 .1 – young	0 0 .1 – bald	0 .1 .2 – light
.5 0 .5 – neutral	0 .5 .5 – middle	0 0 .5 – middle	0 .2 .4 – middle
.9 0 .9 – happy	0 .9 .9 – old	0 0 .9 – full-hair	0 .4 .8 – lots
mood (sad – happy)	age (0 – 100)	amount hair (bald – long)	freckles (some – lots)

What does this encode? 0 .4 .8

If each of n neurons is coding on a scale, at most n distinguishable concepts can be encoded

Decoding with tuning curves

Use spiking rates from multiple neurons to determine encoded feature



- 15 Hz firing rate for red neuron means sound 400 or 800 Hz (at 10 dB)
- 15 Hz for red and 6 Hz for blue requires sound 800 Hz (at 10 dB)

Actual decoding incorporates noise/natural variability in spiking

Population coding to find direction of motion

Non-normalized population coding

- $s_{dir} = \sum_i r_i s_i^{pref}$

r	1	4	1	0	
	↓	→	↑	←	
s^{pref}	$\begin{bmatrix} x \\ y \end{bmatrix} \begin{bmatrix} 0 \\ -1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \end{bmatrix}$	

$s_{dir} =$

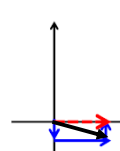
Adding lists of numbers

r	1	4	1	0	
	↓	→	↑	←	
s^{pref}	$\begin{bmatrix} x \\ y \end{bmatrix} \begin{bmatrix} 0 \\ -1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \end{bmatrix}$	$1 \begin{bmatrix} 0 \\ -1 \end{bmatrix} + 4 \begin{bmatrix} 1 \\ 0 \end{bmatrix} + 1 \begin{bmatrix} 0 \\ 1 \end{bmatrix} + 0 \begin{bmatrix} -1 \\ 0 \end{bmatrix} = \begin{bmatrix} 4 \\ 0 \end{bmatrix}$

Population coding to find direction of motion

Non-normalized population coding

- $s_{dir} = \sum_i r_i s_i^{pref}$

r	1	4	1	0	
	↓	→	↑	←	
s^{pref}	$\begin{bmatrix} x \\ y \end{bmatrix} \begin{bmatrix} 0 \\ -1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \end{bmatrix}$	

$\begin{bmatrix} x \\ y \end{bmatrix} = 1 \begin{bmatrix} 0 \\ -1 \end{bmatrix} + 4 \begin{bmatrix} 1 \\ 0 \end{bmatrix} + 1 \begin{bmatrix} 0 \\ 1 \end{bmatrix} + 0 \begin{bmatrix} -1 \\ 0 \end{bmatrix} = \begin{bmatrix} 4 \\ 0 \end{bmatrix}$

Population coding to find direction of motion

“Normalized” firing rate

- $\hat{r}_i = \frac{r_i - r_i^{min}}{r_i^{max} - r_i^{min}}$

If $r^{min} = 1, r^{max} = 6$ for \rightarrow
Then $\hat{r} = \frac{4-1}{6-1} = \frac{3}{5} = 0.6$

Normalized \hat{r} will always be between 0 and 1

r	4	
	→	
s^{pref}	$\begin{bmatrix} x \\ y \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix}$	

Normalized firing rates

$r^{\min}=0 \text{ Hz}, r^{\max}=60 \text{ Hz}$

r	30	30	10	0
	↓	→	↑	←
S^{pref}	$\begin{bmatrix} x \\ y \end{bmatrix} \begin{bmatrix} 0 \\ -1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \end{bmatrix}$

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Population coding to find direction of motion

“Normalized” pop’n coding For \hat{S}_{pop} , divide normalized rate by sum of all rates in neural population: $\sum_j \hat{r}_j$

- $\hat{S}_{pop} = \sum_i \frac{\hat{r}_i}{\sum_j \hat{r}_j} S_i^{pref}$

\hat{r}	0.05	0.5	0.05	0
	↓	→	↑	←
S^{pref}	$\begin{bmatrix} x \\ y \end{bmatrix} \begin{bmatrix} 0 \\ -1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \end{bmatrix}$

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Population coding to find direction of motion

“Normalized” pop’n coding For \hat{S}_{pop} , divide normalized rate by sum of all rates in neural population: $\sum_j \hat{r}_j$

- $\hat{S}_{pop} = \sum_i \frac{\hat{r}_i}{\sum_j \hat{r}_j} S_i^{pref}$

\hat{r}	0.05	0.5	0.05	0
	↓	→	↑	←
S^{pref}	$\begin{bmatrix} x \\ y \end{bmatrix} \begin{bmatrix} 0 \\ -1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \end{bmatrix}$

$\sum_j \hat{r}_j = 0.05 + 0.5 + 0.05 + 0 = 0.6$

Find most-favored

$\begin{bmatrix} x \\ y \end{bmatrix} = \frac{0.05}{0.6} \begin{bmatrix} 0 \\ -1 \end{bmatrix} + \frac{0.5}{0.6} \begin{bmatrix} 1 \\ 0 \end{bmatrix} + \frac{0.05}{0.6} \begin{bmatrix} 0 \\ 1 \end{bmatrix} + 0 \begin{bmatrix} -1 \\ 0 \end{bmatrix} = \begin{bmatrix} 0.83 \\ 0 \end{bmatrix}$ motion direction, do not amplify motion distance

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Another example

Assume for all neurons $r^{\min}=10 \text{ Hz}, r^{\max}=100 \text{ Hz}$

r	50	70	10	30
	↓	→	↑	←
$\begin{bmatrix} x \\ y \end{bmatrix}$	$\begin{bmatrix} 0 \\ -1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \end{bmatrix}$
\hat{r}	$\frac{50-10}{100}$	$\frac{70-10}{100}$	$\frac{10-10}{100}$	$\frac{30-10}{100}$
	0.4	0.6	0	0.2
\hat{r}^{pop}	$\frac{.4}{1.2}$	$\frac{.6}{1.2}$	$\frac{0}{1.2}$	$\frac{.2}{1.2}$
	0.33	0.5	0	0.16
\hat{S}^{pop}	$= \begin{bmatrix} .34 \\ -.33 \end{bmatrix}$			

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A third example

Assume for all neurons $r^{\min}=20 \text{ Hz}, r^{\max}=80 \text{ Hz}$

r	20	20	30	50
	↓	→	↑	←
$\begin{bmatrix} x \\ y \end{bmatrix}$	$\begin{bmatrix} 0 \\ -1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 0 \end{bmatrix}$
\hat{r}	$\frac{20-20}{80}$	$\frac{20-20}{80}$	$\frac{30-20}{80}$	$\frac{50-20}{80}$
	0	0	0.13	0.38
\hat{r}^{pop}	$\frac{0}{.51}$	$\frac{0}{.51}$	$\frac{.13}{.52}$	$\frac{.38}{.51}$
	0	0	.26	.76
\hat{S}^{pop}	$= \begin{bmatrix} -.76 \\ .26 \end{bmatrix}$			

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