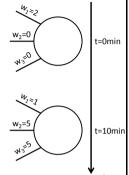
# CISC 3250 Systems Neuroscience

Neuroplasticity: Learning in Neurons

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### Review of weights

RI(t)= $\sum_k w_k \alpha_k(t)$ 

Weights indicate

- Connection (0 or not)
- NT effect
  - w>0 excitatory
  - w<0 inhibitory</pre>
- Magnitude of impact of input

#### Association

We recall information through associations with other information

• Pneumonics:

Roy G. Biv

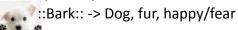
Please Excuse My Dear Aunt Sally () Exp x / + -

• Memories of experiences:

Lake -> Summer vacation 2014

Dealy -> Final exam Fall 2013

Complex objects

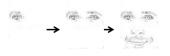


#### Features of associators

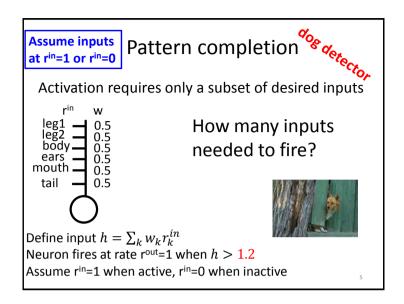
 Pattern completion/ generalization

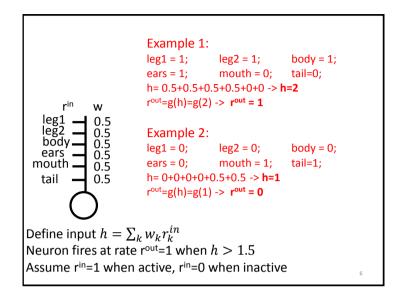


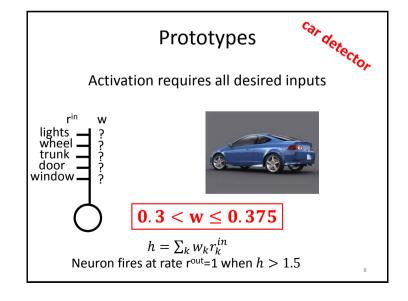
· Learning prototypes

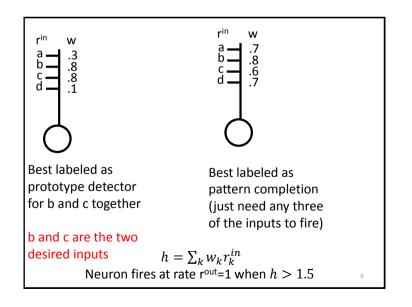


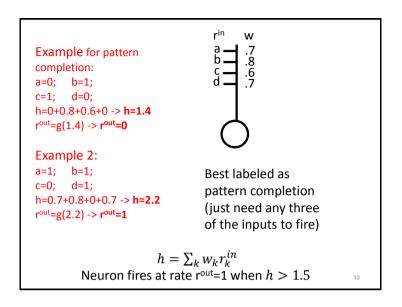
- Neuron firing for common combinations
- Fault tolerance
  - Selected dendrites miss input, post-synaptic neuron still fires

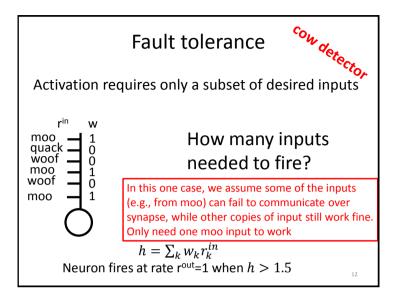




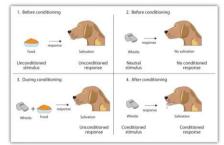






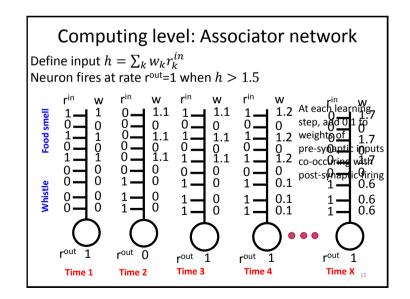


# Learning to associate: Conditioning



Associating both smell and whistle with food

- Unconditioned stimulus: smell already associated with food
- Conditioned stimulus: whistle indicates food coming



#### Two forms of plasticity

- Structural plasticity: generation of new connections between neurons
- Functional plasticity: changing strength of connections between neurons

# **Hebbian plasticity:**

"cells that fire together, wire together"

#### Chemical level: NT receptors

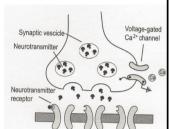
Increase weight by improving NT detection

Post-synaptic:

- Insert more receptors into dendrite membrane
- Improve performance of receptors

Pre-synaptic:

· Increase amount of NT released



# Marr's levels of analysis

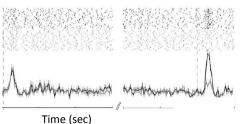
- Computational theory: Learn associations among sensations
- Representation and algorithm: Associate each sense with set of neural outputs, adjust weights on these outputs into another neuron
- Hardware implementation: Insert/remove NT receptors from dendrites

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# Math of Hebbian rate learning

"Cells that fire together, wire together"

$$\begin{array}{ll} \Delta w_{ij} = \epsilon(w) r_i r_j \\ r_j --- r^{\mathrm{in}} & \mathrm{i.e.:} \ \Delta w_{ij} = \epsilon(w) r^{out} r_j^{in} \\ \epsilon & \mathrm{learning \, speed} \end{array}$$



### Using the learning rule

Define input  $h = \sum_k w_k r_k^{in}$  Neuron fires at rate  $r^{\text{out}} = 1$  when h > 1  $\epsilon(w) = \begin{cases} -0.5 & w < 0 \\ 0.5 & w \ge 0 \end{cases} \qquad \Delta w_{ij} = \epsilon(w) r^{out} r_j^{in}$   $\frac{r^{\text{in}}}{1 - 0.5} \quad \frac{w}{1 - 0.5} \quad \frac{1}{1 - 0.5} \quad \frac{$ 

#### Some more math

$$\begin{aligned} w_{j}^{t=2} &= w_{j}^{t=1} + \Delta w_{j}^{t=1} \\ \Delta w_{j}^{t=1} &= \epsilon \left( w_{j}^{t=1} \right) \times r_{out}^{t=1} \times r_{1}^{t=1} \end{aligned}$$

$$w_1^{t=2} = w_1^{t=1} + \Delta w_1^{t=1}$$

$$= w_1^{t=1} + \epsilon (w_1^{t=1}) \times r_{out}^{t=1} \times r_1^{t=1}$$

$$= 0.5 + \epsilon (0.5) \times 1 \times 1 = 0.5 + 0.5 = 1$$

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# Using the learning rule

Define input  $h = \sum_k w_k r_k^{in}$ Neuron fires at rate  $r^{\text{out}}=1$  when h>1

$$\epsilon(w) = \begin{cases} -0.5 & w < 0 \\ 0.5 & w \ge 0 \end{cases} \qquad \Delta w_{ij} = \epsilon(w) r^{out} r_{j}^{in}$$

$$r^{in} \quad w \quad r^{in} \quad r^{in} \quad w \quad r^{in} \quad r^{in} \quad w \quad r^{in} \quad r$$

#### Weight control and decay

- Synaptic weights are finite
- Propose learning rules that keep weights bounded

$$\Delta w_{ij} = r_i r_j - c w_{ij}$$
  
 $\Delta w_i = r_{out} (r_i - w_i)$  Willshaw

 Or, preserve total synaptic weight across network: "normalization"

$$w_j \leftarrow \frac{w_j}{\sum_k |w_k|}$$

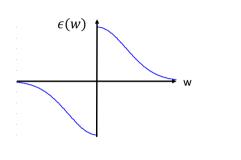
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#### Side note:

#### Weight control with Hebb

$$\Delta w_{ij} = \epsilon(w) r^{out} r_i^{in}$$

• Higher weight – suppressed weight update

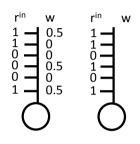


# Using weight control and decay

Define input  $h = \sum_k w_k r_k^{in}$ 

Neuron fires at rate  $r^{out}=1$  when h>1





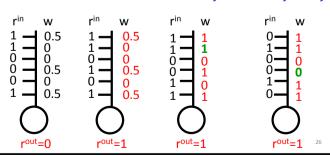




#### Using weight control and decay

Define input  $h = \sum_k w_k r_k^{in}$ Neuron fires at rate  $r^{\text{out}}=1$  when h>1

$$\Delta w_j = r_{out}(r_j - w_j)$$

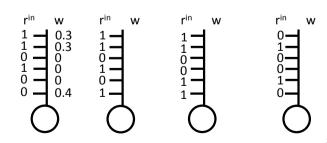


# Using weight control and decay

Define input  $h = \sum_k w_k r_k^{in}$   $\Delta w_j = \epsilon(w_j) r_{out} r_j$  Neuron fires at rate rout=1 when h > .5

$$\epsilon(w) = \begin{cases} -0.5 & w < 0 \\ 0.5 & w \ge 0 \end{cases}$$

$$w_j \leftarrow \frac{w_j}{\sum_k |w_k|}$$



# Using weight control and decay

Define input  $h = \sum_k w_k r_k^{in}$ Neuron fires at rate  $r^{out}=1$  when h > .5  $\epsilon(w) = \begin{cases} -0.5 & w < 0 \\ 0.5 & w \ge 0 \end{cases}$   $w_{ij} \leftarrow \frac{w_{ij}}{\sum_j |w_{ij}|}$   $r^{in} \quad w \quad r^{in} \quad w \quad r^{in} \quad w \quad r^{in} \quad w$   $1 \quad 0.3 \quad 1 \quad 0.32 \quad 1 \quad 0.27 \quad 0 \quad 0.26 \quad 0.27 \quad 0.26 \quad 0.27 \quad 0.26 \quad 0.26 \quad 0.27 \quad 0.26 \quad 0.26 \quad 0.27 \quad 0.26 \quad 0.27 \quad 0.26 \quad 0.26 \quad 0.27 \quad 0.27$ 

#### Hebb + normalization

Step 1: Compute output at time t

Step 2: Use Hebb learning based on  $r_{out}^t$ ,  $w_j^t$ ,  $r_j^t$  to find new  $w_i^{t+1}$ 's

Step 3: Divide new  $w_j^{t+1}$ 's by  $\sum_k |w_k^{t+1}|$  so new  $|w_i|$ 's add to 1

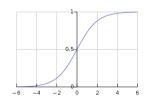
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# Al Neural Net Learning

Computed output:  $g^{\text{sigmoid}}(\sum_{i} w_i r_i^{in})$ 

Desired output:  $y^{out} \in [0,1]$ 

•  $\Delta w_i = \epsilon r_i^{in} r^{out} (y^{out} - r^{out}) (1 - r^{out})$ 



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rout=0 28

