Example questions

In how many ways can 1 gold, 1 silver, and 1 bronze metal be awarded to 10 contestants?

How many ways are there to select 3 class representatives from a class of 25 students?

You can borrow up to 3 DVDs from your friends, who owns 30 DVDs.

- How many ways are there to select 1 DVD?
- How many ways are there to select 2 DVDs?
- How many ways are there to select 3 DVDs?
- How many ways are there to select 3 or fewer DVDs?

There are 8 songs you can play at your party. How many ways are there to select a play list containing 5 of these songs (where the order matters)? P(8,5)=8x7x6x5x4=6720

You are taking a multiple choice test where each question has 5 possible answers to choose from --- A, B, C, D, or E --- and there are 4 questions in total.

- How many possible ways are there to select your answers?
- How many ways are there to select answers if no letter can be used for more than one question?

P(5,4)=5x4x3x2=**120**

- How many ways are there to select answers if the fourth answer must by the same as the first?
- How many ways are there to select answers if one letter is used for two of the answers and the remaining answers use distinct letters?
 Ways with first two letters same, second two different (|SSDD|) + |SDSD| + |SDDS| + |DSSD| + |DSSS| + |DSSS| + |DSSS| = 5x1x4x3 + 5x4x1x3 + 5x4x3x1 + 5x4x3x1 + 5x4x3x1 = 360

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- in hardcover and in paperback
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How many ways can you order the computer science book? 2x2x3x3=**36**

I am forming a Fordham Jeopardy team and need to select 6 members. I have 7 candidates from the Computer Science department, 9 from the Economics department, 10 from the English department, and 12 from the Theater department.

(Give the expression to find the answers, actual number is welcome but not required)

- How many ways can I choose from all the candidates? $C(70,6) = \frac{70!}{64!7!} = \frac{70\times69\times68\times67\times66\times65\times64}{7\times6\times5\times4\times3\times2\times1} = \frac{69\times68\times67\times66\times65\times64}{6\times4\times3} = 1,198,774,720$ $C(38,6) = \frac{38!}{32!6!} = \frac{38\times37\times36\times35\times34\times33}{6\times5\times4\times3\times2\times1} = 2,760,681$
- How many ways can I choose a team where all members are from the same department?
- How many ways can I choose a team with 2 computer science students, 2 economics students, and 2 theatre students?
- How many ways can I choose a team with no computer science majors?

Solve for: P(3,1)= 3		
P(4,2)		
P(5,2)		
P(m,0)= 1		
C(5,3)		
C(4,1)		
C(4,4)		

You are given an exam with every question having either the answer "true" or "false." There are 10 questions on the exam and you guess randomly for each question. Assuming each answer is equally likely to be true or false:

• What is the probability you get exactly 5 questions correct? Number of arrangements of TTTTTFFFFF = $\frac{10!}{5!5!} = \frac{10 \times 9 \times 8 \times 7 \times 6}{5 \times 4 \times 3 \times 2 \times 1} = \frac{9 \times 8 \times 7 \times 6}{4 \times 3 \times 2} = \frac{9 \times 7 \times 6}{3} = 9 \times 7 \times 2 = 126$ 252 Number of possible arrangements: $2^{10} = |S|$ $\frac{C(10,5)}{2^{10}} = \frac{252}{1024} \approx .246$ • What is the probability you get fewer than 8 questions correct?

You have a jar of jelly beans in front of you containing 20 cherry, 10 orange, 15 lemon, 15 watermelon, and 10 grape flavor. You take 5 beans without looking. (Give the expression to find the answers, actual number/fraction is welcome but not required):

- What is the probability you pick one of each flavor? $\frac{\frac{20 \times 10 \times 15 \times 15}{70 \times 69 \times 68 \times 67 \times 66} \approx .00003}{20 \times 10 \times 15 \times 15} = \frac{20 \times 10 \times 15 \times 15}{2,017,169} \approx .0223$
- What is the probability none of the picked beans are cherry?

We go to the casino and play a dice-rolling game. Each die is 6 sided and 3 die are rolled.

- What is the probability all 3 die roll higher than 4?
- What is the probability at least one 3 is rolled?
- What is the probability all 3 rolls are different?

$$\frac{6\times5\times4}{6\times6\times6} = \frac{120}{216} = \frac{5}{9} \approx .556$$

- What is the probability the first 2 dice rolled add up to 2 or 5? (1,1),(1,4),(2,3),(3,2),(4,1) $\frac{5}{6\times 6} = \frac{5}{36} \approx .139$
- What is the probability the first roll is even or greater than 4?
- What is the probability the second roll is a multiple of 2 or of 3?

I flip a biased coin where it will land on heads with 2/3 probability.

- What is the probability of getting 2 tails in 2 flips? Prob(first tail)xProb(second tail)= $\left(1-\frac{2}{3}\right) \times \left(1-\frac{2}{3}\right) = \frac{1}{3} \times \frac{1}{3} = \frac{1}{9} \approx .111$
- What is the probability of getting all heads in 4 flips?
- What is the probability of getting fewer than 2 tails in 4 flips?