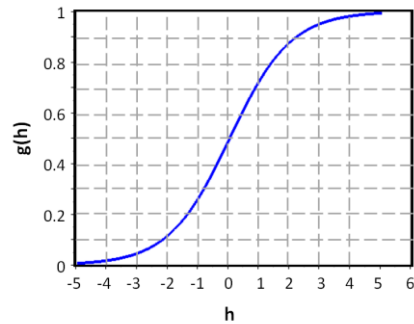
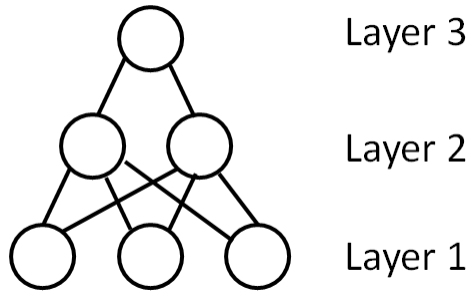


Final practice part 2

1. Consider the neural network below.



The initial weights are:

Layer 1:	$w_{1,1}^1 = -10$	$w_{1,2}^1 = 0$	$w_{1,3}^1 = -5$	$w_{1,4}^1 = 10$	$b_1^3 = 4$	Unit 1
	$w_{2,1}^1 = 20$	$w_{2,2}^1 = 0$	$w_{2,3}^1 = 10$	$w_{2,4}^1 = -5$	$b_1^3 = 4$	Unit 2
	$w_{3,1}^1 = 0$	$w_{3,2}^1 = -10$	$w_{3,3}^1 = 0$	$w_{3,4}^1 = 20$	$b_1^3 = 4$	Unit 3
Layer 2:	$w_{1,1}^2 = 5$	$w_{1,2}^2 = 10$	$w_{1,3}^2 = 0$	$b_1^3 = -2$		Unit 1
	$w_{2,1}^2 = 0$	$w_{2,2}^2 = -10$	$w_{2,3}^2 = 15$	$b_1^3 = -2$		Unit 2
Layer 3:	$w_{1,1}^3 = 10$	$w_{1,2}^3 = -20$	$b_1^3 = 5$			

Compute the output given the following inputs:

(a) Compute r_1^1, r_2^1, r_3^1 . Given the inputs: $x_1=5$ $x_2=-10$ $x_3=10$ $x_4=0$

(b) Compute r_1^3 . Given the lower-layer outputs: $r_1^2=0.1$, $r_2^2=0.6$

(c) Compute r_2^2 . Given the lower-layer outputs: $r_1^1=0.1$, $r_2^1=0.3$, $r_3^1=0.6$

Compute the change in the specified weight based on the following input/outputs. In each case, presume the starting weight is as specified in the original list above. Assume $\epsilon = 1$

(d) Compute $\Delta w_{1,2}^3$. Given the layer 2 rates: $r_1^2=0.2$ and $r_2^2=0.8$; layer 3 rates: $r_1^3=0.1$; the desired output from r_1^3 is 1.0

(e) Compute $\Delta w_{1,2}^1$. Given the features: $x_1=10$, $x_2=-5$, $x_3=0$, $x_4=15$; $r_1^1=0.5$, $r_2^1=0.2$, $r_3^1=0.8$; delta values: $\delta_1^2 = -0.005$, $\delta_2^2 = 0.01$

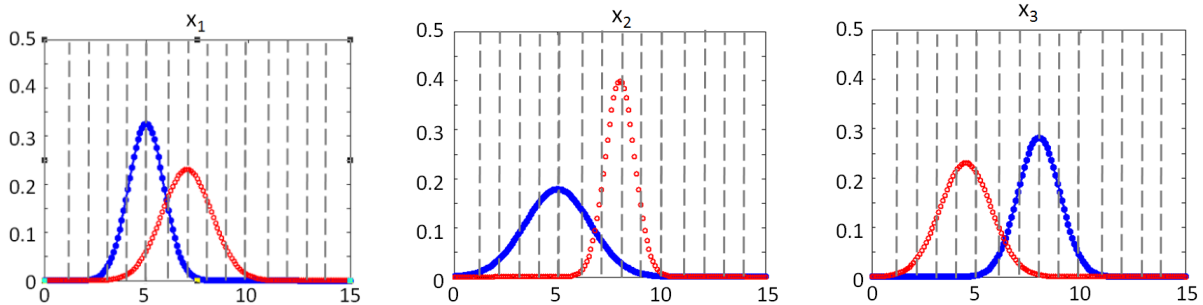
2. For each of the following functions $f(x; h)$, compute the value of h that will maximize $f(x; h)$, assuming each function has a single maximum and no minimum.

(a) $f_1(\mathbf{x}; h) = \sum_i (-h^2 - 10hx_i + 12x_i^2)$

(b) $f_2(x; h) = e^{-(h^3+x^2)} = \exp(-(h^2 + x^2))$

(c) $f_3(\mathbf{x}; h) = \prod_i 3h^{(x^i)}$

3. Consider the following Gaussian likelihoods for features x_1 , x_2 , and x_3 given **class = 1** (blue curves) or **class = 0** (red curves).



i. We wish to multiply these likelihoods together to compute $P(\mathbf{x} | y)$. Which type of classification is this:

- (a) Naïve Bayes Max-Posterior classification
- (b) Non-Naïve Bayes Max-Likelihood classification
- (c) Naïve Bayes Max-Posterior classification
- (d) Naïve Bayes Max-Likelihood classification
- (e) Support Vector Machine classification

ii. For the feature values below, which class is more probable (based on $P(\mathbf{x} | y)$ calculated from the plots above)?

(a) $x_1=5$ $x_2=7$ $x_3=6$

(b) $x_1=8$ $x_2=8$ $x_3=6$

iii. Which class is more probable if we also incorporate the following prior:

$$P(y=0) = 0.1 \quad P(y=1) = 0.9$$

to compute $P(y|\mathbf{x})$?

(a) $x_1=4$ $x_2=5$ $x_3=9$

(b) $x_1=6$ $x_2=7$ $x_3=7$

iv. Provide a prior that would make class 1 more probable if the \mathbf{x} values are:

$x_1=6$ $x_2=8$ $x_3=6$

4. Using each of the following kernel functions, compute the result of $K(\mathbf{x}^1, \mathbf{x}^2)$, for the specified input vectors.

$$K(\mathbf{c}, \mathbf{d}) = 2^{-(\mathbf{c}^T \mathbf{d} + 2)}$$

(a) $\mathbf{c} = \begin{bmatrix} 4 \\ 0 \\ -2 \end{bmatrix}$ $\mathbf{d} = \begin{bmatrix} 0 \\ 0 \\ 1.5 \end{bmatrix}$

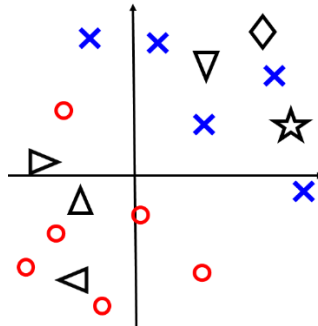
(b) $\mathbf{c} = \begin{bmatrix} 1 \\ 0.5 \\ -2 \end{bmatrix}$ $\mathbf{d} = \begin{bmatrix} 3 \\ -2 \\ -1 \end{bmatrix}$

$$K(\mathbf{c}, \mathbf{d}) = (\mathbf{c}^T \mathbf{d} - 4)^2 + 10\mathbf{c}^T \mathbf{d}$$

(c) $\mathbf{c} = \begin{bmatrix} 0 \\ 3 \\ -2 \end{bmatrix}$ $\mathbf{d} = \begin{bmatrix} 1 \\ 0 \\ 2 \end{bmatrix}$

(d) $\mathbf{c} = \begin{bmatrix} -1 \\ 2 \\ -1 \end{bmatrix}$ $\mathbf{d} = \begin{bmatrix} 3 \\ 0 \\ -1 \end{bmatrix}$

5. Consider the following training data. Red circles are class 0, blue x's are class 1, and all other shapes (triangles, stars, diamonds) are data points with known feature values but unknown labels.



Using the EM approach for learning, and assuming that we use a linear logistic classifier, how will the black triangles, diamonds, and star data points be used for learning? In the first round of EM, what y value do you expect each data point to be assigned, or no value at all?

6. Consider the classification problem with the following features and classes.

Class **P**erson-type: Teenager, YoungProfessional, Adult, SeniorCitizen

Features:

Daily-time-online: 1-2 hours, 3-4 hours, 5-8 hours

Number-of-online-friends: 0-10, 10-50, 50-200, 200-1000

Favored content: News, SocialPosts, Education, Entertainment

Money-spent-online: None, \$1-\$50, \$50-\$100, \$100-\$500, \$500+

(a) How many parameters given Naïve Bayes a posteriori classification?